PROSPECT-D: Towards modeling leaf optical properties through a complete lifecycle

J.-B. Féret, A.A. Gitelson, S.D. Noble, S. Jacquemoud

Abstract

Leaf pigments provide valuable information about plant physiology. High resolution monitoring of their dynamics will give access to better understanding of processes occurring at different scales, and will be particularly important for ecologists, farmers, and decision makers to assess the influence of climate change on plant functions, and the adaptation of forest, crop, and other plant canopies. In this article, we present a new version of the widely-used PROSPECT model, hereafter named PROSPECT-D for dynamic, which adds anthocyanins to chlorophylls and carotenoids, the two plant pigments in the current version. We describe the evolution and improvements of PROSPECT-D compared to the previous versions, and perform a validation on various experimental datasets. Our results show that PROSPECT-D outperforms all the previous versions. Model prediction uncertainty is decreased and photosynthetic pigments are better retrieved. This is particularly the case for leaf carotenoids, the estimation of which is particularly challenging. PROSPECT-D is also able to simulate realistic leaf optical properties with minimal error in the visible domain, and similar performances to other versions in the near infrared and shortwave infrared domains.

1. Introduction

Climate change is expected to affect vegetation worldwide, influencing air temperature, biogeochemical cycles, and the frequency and intensity of plant disease. Leaf pigments are key components of life on Earth: they are major contributors to individual plant health via complex mechanisms allowing photosynthesis, plant growth, protection, adaptation to environmental changes and phenological events. Their dynamics directly affects nutrient, nitrogen, carbon and water cycles. Leaf pigments are therefore important for ecologists, farmers, and decision makers to assess the influence of climate change on plant functions, and the adaptation of forest, crop, and other plant canopies. In this article, we present a new version of the widely-used PROSPECT model, hereafter named PROSPECT-D for dynamic, which adds anthocyanins to chlorophylls and carotenoids, the two plant pigments in the current version. We describe the evolution and improvements of PROSPECT-D compared to the previous versions, and perform a validation on various experimental datasets. Our results show that PROSPECT-D outperforms all the previous versions. Model prediction uncertainty is decreased and photosynthetic pigments are better retrieved. This is particularly the case for leaf carotenoids, the estimation of which is particularly challenging. PROSPECT-D is also able to simulate realistic leaf optical properties with minimal error in the visible domain, and similar performances to other versions in the near infrared and shortwave infrared domains.

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they have been called the “Nature’s Swiss army knife” by Gould (2004). Among the identified functions of anthocyanins are the protection of the photosynthetic apparatus from damage due to excess light (Lee and Gould, 2002), environmental stresses such as freezing or air pollution, plant pathogens, and predation (Lev-Yadun and Gould, 2008). An exhaustive review of the role of anthocyanins in plant leaves can be found in (Davies, 2004) and (Gould, 2004).

Leaf pigments interact with solar radiation and change in response to environmental conditions to optimize plant metabolism following complex pathways, within constraints of available resources and stressors. As a result, leaf optical properties are directly impacted by the composition of pigments. Remote sensing has proved to be a particularly suitable tool for the estimation of leaf pigments, both at level of the leaf (e.g., Féret et al., 2008; Gitelson et al., 2006; le Maire et al., 2004; Richardson et al., 2002; Sims and Gamon, 2002) and the canopy (e.g., Asner et al., 2015b; Atzberger et al., 2010; Gitelson et al., 2005; Haboudane, 2004; Hmimina et al., 2015). The retrieval of pigment content from remote sensing data involves two main approaches. The first approach is data-driven. It includes univariate statistical models derived from spectral indices (e.g., Gitelson et al., 2006), multivariate statistical models such as partial least squared regressions (e.g., Asner and Martin, 2009) and machine learning algorithms (e.g. Verrelst et al., 2015). The relationships derived from these predictive models are usually established empirically; they strongly depend on the variability and quality of the data used to adjust these models, therefore they may lack robustness. The second approach is based on radiative transfer models that exist both at leaf and canopy scales. Leaf models generally simulate their spectral directional-hemispherical reflectance and transmittance while canopy models simulate their spectral and bidirectional reflectance assuming that the leaf and soil optical properties, the vegetation architecture, and the conditions of acquisition are known. The combination of the two approaches (data-driven and physical) is also becoming increasingly popular because it provides alternatives to extensive data collection required by the first, and high computational resources required by the second (Féret et al., 2011; Verrelst et al., 2015).

To date, most studies devoted to vegetation pigments have focused on chlorophyll. This can be explained by multiple factors. First, leaf chlorophyll content is the variable that has the strongest effect on canopy reflectance in the VIS, and is a valuable proxy of nitrogen content and gross primary production (e.g., Gitelson et al., 2012; Peng and Gitelson, 2012), which have strong impact in terms of food and biomass production globally. Second, leaf chlorophyll content can be estimated with relatively good accuracy using simple statistical regression models based on the relationship between this variable and various spectral indices (e.g. Féret et al., 2011; Gitelson et al., 2006; le Maire et al., 2004). Third, the availability of physical models including chlorophyll as input parameters allowed investigating and better understanding its influence on the signal measured by satellite sensors, leading to improved predictive models for leaf and canopy chlorophyll content in a more systematic way than experimental data collection would have permitted. This is the case of the combined PROSPECT leaf optical properties model (Jacquemoud and Baret, 1990) and SAIL canopy bidirectional reflectance model (Verhoef, 1984; Verhoef et al., 2007), also referred to as PROSAIL, which has been used for >25 years (Jacquemoud et al., 2009).

Current challenges such as food security, global warming and massive biodiversity loss now require fine monitoring of vegetation status, with a level of information beyond inputs provided by chlorophyll content alone. We need to address various issues related to vegetation, including stress, invasive species, plant diseases and photosynthetic phenology, which implies monitoring the dynamic of various pigment types such as carotenoids (Gamon et al., 2016) and anthocyanins. One of the most studied “pigment-related” indicators derived from remote sensing is the Photochemical Reflectance Index (PRI, Gamon et al., 1992) based on two narrow spectral bands in the green spectrum: the PRI related to the xanthophyll cycle in the leaf; it captures the physiological response of vegetation in response to a short term environmental stress inducing slight changes in photosynthetic activity (Gamon et al., 1992, 1999, 1997). However, the primary driver of the PRI over long time periods, at both leaf and canopy scales, is not the xanthophyll cycle, but rather the changing leaf carotenoid pigment pool, typically expressed as the changing ratio of chlorophyll to carotenoid pigments (or its inverse) (Filippa et al., 2009; Nakaji et al., 2006; Stylianski et al., 2002). Therefore, information about pigment content in vegetation is crucial when monitoring photosynthetic phenology. At local scale, estimating pigment content from individuals using portable devices, close range remote sensing or UAV can be useful for monitoring purposes in precision agriculture or ecophysiology. At global scale, the ability to precisely monitor photosynthetic phenology with satellite imagery is extremely valuable and would provide important input for models of global terrestrial carbon uptake. Few studies focus on the direct estimation of carotenoids at leaf scale (Chappelle et al., 1992; Gitelson et al., 2001, 2006; Sims and Gamon, 2002) and canopy scale (Asner et al., 2015a, 2015b; Gamon et al., 2016; Hernández-Clemente et al., 2012, 2014; Ustin et al., 2009; Zarco-Tejada et al., 2013). Even fewer focus on the estimation of anthocyanin, also at leaf (Gamon and Surfas, 1999; Gitelson et al., 2001, 2006; Sims and Gamon, 2002; Steele et al., 2009) and canopy (Rundquist et al., 2014) scales. The presence of overlapping features in the specific absorption coefficient (SAC) of carotenoids and anthocyanins makes it difficult to separate and quantify these accessory pigments using basic methods such as spectral indices, especially at canopy scale (Ustin et al., 2009).

Monitoring vegetation status, stress, and shifts in the ecosystem functional properties is critical. It will require sophisticated methods of leaf pigment content estimation, possibly combined with the next generation of high resolution imaging spectrometers like Hypars (NASA), EnMAP (DLR) or Hypoxim (CNES), and vegetation radiative transfer models that incorporate all major pigments. Present leaf optical properties models do not include pigments other than chlorophylls and carotenoids, limiting the application of the physical approach to the study of these pigments (Blackburn, 2007). SLOP (Maier et al., 1999), PROSPECT-5 (Féret et al., 2008), and soon after LIBERTY, specifically designed for pine needles (Di Vittorio, 2009), are the three models that use carotenoids. The dorsiventral leaf model designed by Stuckens et al. (2009) also differentiates chlorophylls from carotenoids, but the SACs are those used in PROSPECT-5.

This article introduces a new version of the widely-used PROSPECT model, called PROSPECT-D, which for the first time includes all three main pigments that control the optical properties of fresh leaves, i.e., chlorophylls, carotenoids, and anthocyanins. The suffix -D stands for “dynamic” because the model makes it possible to simulate leaf optical properties through a complete lifecycle, from emergence, to anthocyanin-expressing stress responses, through to senescence. Given the success and widespread use of PROSPECT-5, a major requirement for the development of PROSPECT-D was to preserve, and ideally to improve on, the performance of PROSPECT-5 for pigment estimation in samples containing little or no anthocyanin, while adding support for those that do. We performed a new calibration of the SAC of each pigment, and updated the refractive index used by the model. PROSPECT-D was then tested on several datasets displaying many plant species with a large range of leaf traits including pigment composition. We evaluated its performance using two criteria resulting from iterative optimization of leaf chemical and structural properties: the difference between the measured and the modeled leaf directional-hemispherical reflectance and transmittance spectra, and the accuracy of corresponding pigment estimation. We compared these two criteria for the new and current versions of the model.

2. Calibration of the model

Several strategies for the calibration of PROSPECT have been investigated since its first version. All of the procedures have points in common, such as the adjustment of one or several optical constants (SAC
of leaf chemical constituents, refractive index) over the VIS, near infrared and shortwave infrared (SWIR) domains. A standard method consists in determining the optical constants individually or simultaneously at each wavelength by using an iterative procedure (Féret et al., 2008; Li and Wang, 2011). So far, there is no unique method, and adaptations have been proposed to calibrate PROSPECT: Malenovský et al. (2006) adjusted SACs for needle-shaped leaves; Féret et al. (2008) have simultaneously determined the refractive index and SAC of leaf constituents; Chen and Weng (2012) have computed an individual refractive index for each leaf sample. In this section, we provide information about the calibration of PROSPECT-D, including the selection of the calibration dataset, as well as the main steps leading to updated optical constants.

2.1. Available datasets

Six independent datasets collected by several researchers for diverse purposes have been used in this study (Table 1). They share directional-hemispherical reflectance and/or transmittance spectra, and at least two pigments out of three (chlorophylls, carotenoids, and anthocyanins) measured using wet chemistry. The ANGERS dataset includes >40 plant species; all the other datasets are monospecies: European hazel (Corylus avellana L.) in HAZEL, Norway maple (Acer platanoides L.) in MAPLE, Virginia creeper (Parthenocissus quinquefolia (L.) Planch) in VIRGINIA, and Siberian dogwood (Cornus alba L.) in DOGWOOD-1 and -2. Table 1 summarizes the spectral and chemical information available for each dataset. Additional information about the protocols used to conduct the experiments, collect the leaves, measure their optical properties and determine their wet chemistry can be found in (Féret et al., 2008; Gitelson et al., 2001, 2006, 2009; Merzlyak et al., 2008). Note that DOGWOOD-2 does not contain transmittance spectra; that the total chlorophyll content (C_{ch} \text{expressed in } \mu g \text{ cm}^{-2}) is available in all datasets; that the total carotenoid content (C_{car} \text{expressed in } \mu g \text{ cm}^{-2}) and the total anthocyanin content (C_{anth} \text{expressed in } \mu g \text{ cm}^{-2}) have not been determined in HAZEL and ANGERS, respectively. Finally, the 400–780 nm spectral range used for the calibration of the pigment content is common to all datasets except DOGWOOD-1.

<table>
<thead>
<tr>
<th>Database</th>
<th>Reference</th>
<th>Spectral range (nm)</th>
<th>Number of leaves</th>
<th>Optical properties</th>
<th>Chlorophyll content C_{ch} (\mu g \text{ cm}^{-2})</th>
<th>Carotenoid content C_{car} (\mu g \text{ cm}^{-2})</th>
<th>Anthocyanin content C_{anth} (\mu g \text{ cm}^{-2})</th>
</tr>
</thead>
<tbody>
<tr>
<td>ANGERS*</td>
<td>1, 2</td>
<td>400–2500</td>
<td>308</td>
<td>R &amp; T</td>
<td>34.41 ± 21.85 0.78</td>
<td>106.70 ± 3.14 0.00</td>
<td>8.84 ± 5.14 0.00</td>
</tr>
<tr>
<td>VIRGINIA</td>
<td>3, 4</td>
<td>400–800</td>
<td>81</td>
<td>R &amp; T</td>
<td>11.05 ± 14.60 0.09</td>
<td>53.76 ± 0.61 0.05</td>
<td>2.98 ± 3.06 0.15</td>
</tr>
<tr>
<td>MAPLE</td>
<td>3, 4, 6</td>
<td>400–780</td>
<td>48</td>
<td>R &amp; T</td>
<td>7.43 ± 7.36 0.14</td>
<td>32.98 ± 0.61 0.05</td>
<td>5.25 ± 2.37 1.82</td>
</tr>
<tr>
<td>DOGWOOD-1</td>
<td>3, 4, 5</td>
<td>440–796</td>
<td>20</td>
<td>R &amp; T</td>
<td>4.53 ± 4.84 0.07</td>
<td>15.03 ± 0.61 0.05</td>
<td>2.96 ± 2.06 0.42</td>
</tr>
<tr>
<td>HAZEL</td>
<td>3, 4</td>
<td>400–800</td>
<td>13</td>
<td>R &amp; T</td>
<td>26.37 ± 3.55 22.69</td>
<td>34.62 ± 0.61 0.05</td>
<td>N/A</td>
</tr>
<tr>
<td>DOGWOOD-2</td>
<td>6</td>
<td>400–1000</td>
<td>51</td>
<td>R</td>
<td>23.77 ± 7.58 1.53</td>
<td>39.81 ± 0.61 0.05</td>
<td>5.39 ± 2.26 1.73</td>
</tr>
</tbody>
</table>

1: Féret et al. (2008); 2: Féret et al. (2011); 3: Merzlyak et al. (2008); 4: Gitelson et al. (2009); 5: Gitelson et al. (2001); 6: Gitelson et al. (2006).

Fig. 1. Relationship between C_{anth} obtained from wet chemistry and C_{anth} estimated from reflectance data after application of Eq. (2). The black dots correspond to the 137 leaf samples with mARI<5 (R² = 0.90) and the grey dots correspond to the 76 leaf samples with mARI>5 (R² = 0.37). Eq. (2) was adjusted only on the black dots.
2.2.1. Estimation of leaf anthocyanin content in ANGERS

Several nondestructive methods to estimate \( C_{\text{anth}} \) from leaf reflectance have been identified and tested on experimental data for which the anthocyanin content has been measured. These methods included spectral indices and machine learning algorithms such as support vector regression (Gitelson et al., 2001, 2006, 2009; van den Berg and Perkins, 2005; Pfündel et al., 2007). The modified Anthocyanin Reflectance Index (mARI) designed by Gitelson et al. (2006) led to the best results when using a leave-one-out cross-validation. This index is defined by:

\[
mARI = \left( \frac{R_{\text{green}}^{-1}-R_{\text{red edge}}^{-1}}{R_{\text{NIR}}} \right) \times R_{\text{NIR}}
\]

where \( R_{\text{green}} \) is the mean reflectance between 540 nm and 560 nm, \( R_{\text{red edge}} \) the mean reflectance between 690 nm and 710 nm, and \( R_{\text{NIR}} \) the mean reflectance between 760 nm and 800 nm. We first studied the relationship between \( mARI \) and \( C_{\text{anth}} \) over the 213 samples for which information about anthocyanins was available, i.e., all datasets of Table 1 with the exception of ANGERS. We found a strong linear relationship for \( mARI \) values smaller than 5 (137 samples, \( R^2 = 0.90 \), RMSE = 1.18 \( \mu \)g cm\(^{-2} \)) and a weak one for \( mARI \) values >5 (76 samples, \( R^2 = 0.37 \), RMSE = 6.35 \( \mu \)g cm\(^{-2} \)) (Fig. 1). These samples with \( mARI < 5 \) correspond to mature green, yellow, and reddish/red leaves with \( C_{\text{anth}} \) values <12 \( \mu \)g cm\(^{-2} \). Leaves with \( C_{\text{anth}} \) values higher than 12 \( \mu \)g cm\(^{-2} \) are generally dark red and contain small amounts of chlorophyll. In that case, absorbance between 540 nm and 560 nm exceeded 90% and further increases of anthocyanin did not change leaf optical properties. A linear model for anthocyanin estimation (Eq. (2)) was then derived from the subset excluding the samples with \( mARI > 5 \) and \( C_{\text{anth}} > 12 \mu \)g cm\(^{-2} \).

\[
C_{\text{anth}} = 2.11 \times mARI + 0.45
\]

Eq. (2) was applied to the ANGERS dataset to determine \( C_{\text{anth}} \). The anthocyanin content ranged from 0 to 17.1 \( \mu \)g cm\(^{-2} \), with a mean value of 1.7 \( \mu \)g cm\(^{-2} \).

2.2.2. Selection of the calibration samples

In order to keep as many samples as possible, we decided to build a calibration dataset made of leaf samples selected both in ANGERS and VIRGINIA. The influence of the uncertainty associated to \( C_{\text{anth}} \) in ANGERS is expected to be mitigated by the accuracy of \( C_{\text{anth}} \) in VIRGINIA.

In VIRGINIA we identified samples characterized by low \( \text{Cab} \) (<20 \( \mu \)g cm\(^{-2} \)) and \( \text{Ce} \) (<5 \( \mu \)g cm\(^{-2} \)) in order to decrease the combined influence of the pigments on leaf optical properties, but also to minimize the correlation among pigments. It should allow capturing the influence of anthocyanins independently from the other pigments. We randomly selected 20 samples, leaving a total of 61 samples of VIRGINIA for the validation.

In ANGERS we discarded at first 14 atypical samples, the spectral behavior of which was incompatible with PROSPECT assumptions. For example, we removed samples collected on *Eucalyptus gunnii* and *Cornus alba*, the overall reflectance of which was very high in the VIS because of the presence of wax (Barry and Newnham, 2012); and three samples of *Schefflera arboricola* displaying uncharacteristic optical properties in the blue (400–450 nm). We also removed samples with \( mARI > 5 \) as the uncertainty associated to \( C_{\text{anth}} \) was particularly high (Fig. 1). Finally we eliminated leaf samples that had little influence on the calibrated SACs. For that purpose we determined a reference SAC for each pigment using the 314 preselected leaf samples (20 from VIRGINIA and 294 from ANGERS). The ANGERS samples inducing changes in the SACs higher than 5% between 425 nm and 475 nm were kept in the calibration dataset made of leaf samples selected both in ANGERS and VIRGINIA. The influence of the uncertainty associated to \( C_{\text{anth}} \) in ANGERS is expected to be mitigated by the accuracy of \( C_{\text{anth}} \) in VIRGINIA.

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In total, a dataset named CALIBRATION and combining subsets of ANGERS (144 samples) and VIRGINIA (20 samples) was used for the calibration phase.
2.2.3. Sensitivity of the calibration to the uncertainty associated with Canth in ANGERS

As abovementioned, determining Canth with a spectral index like mAARI leads to uncertainty likely to impact the quality of the calibration. We performed a sensitivity analysis with the aim of understanding the influence of this uncertainty on the SACs and on the overall performances of the model. It consisted in adding a Gaussian noise (σ = 1.18 μg cm⁻²) to Canth in ANGERS prior to the calibration and validation procedure. We repeated the operation 50 times.

2.3. Selection of the refractive index

PROSPECT is based on the generalized plate model proposed by (Allen et al., 1969, 1970). A plant leaf is modeled as a pile of elementary layers characterized by an absorption coefficient and a refractive index provided at a given wavelength. In the first version of the model, Jacquemoud and Baret (1990) used an albino maize leaf to obtain an experimental spectrum of the refractive index for the elementary layers. Le Maire et al. (2004) and Féret et al. (2008) adopted a new strategy based on numerical optimization to determine the optical constants of PROSPECT at the same time. Their refractive index performed slightly better than the previous versions at estimating leaf chemical constituents, but the strong spectral variations observed in the visible wavelengths induced small artifacts in the optical properties of leaves displaying high pigment content. Stuckens et al. (2009) also adjusted a unique refractive index for all leaves.

Attempts to obtain a unique refractive index spectrum for all leaves are actually unfounded and inconsistent with the Kramers-Kronig relations that state that the real (refractive index) and imaginary (absorption coefficient) parts of the complex refractive index of a medium are physically linked (Lucarini et al., 2005). These relations allow direct computation of the refractive index of a medium based on its absorption properties on an extended spectral domain. Chen and Weng (2012) used the Kramers-Kronig relations to derive an effective refractive index adjusted to each leaf sample, obtaining very promising results. However, leaf chemical and spectral databases are often incomplete; in particular they cover a limited range of the electromagnetic spectrum, so such a method is impracticable. As a consequence we considered the evident refractive index to be independent of the leaf sample in this study, but changed strategy compared to PROSPECT-5 in order to avoid the abovementioned artifacts resulting from numerical optimization. Two options were tested: 1) using the refractive index imbedded in PROSPECT-3, and 2) taking the average refractive index derived from minimum and maximum values computed by Chen and Weng (2012) and corresponding to the boundaries of the grey area in Fig. 2. The spectra displayed in Fig. 2 strongly differ in shape in the VIS: the overall profile of the refractive indices computed by Chen and Weng (2012) is quite similar to that measured for pure liquid water (Hale and Querry, 1973), gradually decreasing from the visible to the infrared, whereas the indices in PROSPECT-3 and -5 are very much alike in the near and shortwave infrared (1000–2500 nm) and show a steeper decrease. Divergence between the refractive index derived from Chen and Weng (2012) and those used in PROSPECT-3 and -5 strongly increases with wavelength. We performed the full calibration of PROSPECT (including optimal adjustment of SAC as described in Section 2.4) with each refractive index.

2.4. Optimal adjustment of the specific absorption coefficients

The adjustment of the SAC for each group of pigments is based on numerical optimization routines applied to experimental data. As in PROSPECT-5 we assumed that the chlorophyll a:b ratio was constant and we combined carotenes and xanthophylls in the carotenoid group. Similarly anthocyanins were assumed to include all types of anthocyanins contributing to light absorption in the VIS. Given the well-known sensitivity of the anthocyanin absorption properties to pH, which is due to a reversible structural change that occurs in the C ring of the molecule, this hypothesis may be incorrect in certain situations. However, environment inside a vacuole is generally slightly acid, with pH values reported to fall within the range of 5.0 to 6.0 pH units, with a mean pH of 5.5 (Mathieu et al., 1989; Martinière et al., 2013).

Solved SAC values were constrained to be positive. To prevent erroneous absorption assignments, the wavelength domains were narrowed to 400–750 nm for chlorophylls, 400–560 nm for carotenoids, and 400–660 nm for anthocyanines. These ranges are broader than those in vitro due to the detour effect: the lengthening of the optical path-length within the leaf results in substantial flattening of the absorption spectrum in vivo (e.g., Rühle and Wild, 1979; Fukushima et al., 1993).

![Fig. 4. Spectral RMSE between measured leaf optics and simulated reflectance (left), and transmittance (right) obtained after model inversion with the refractive index used in PROSPECT-5 (black dotted line), PROSPECT-3 (red), and derived from Chen and Weng (2012) (light grey).](image-url)

![Fig. 5. Specific absorption coefficients of chlorophylls (green), carotenoids (orange), and anthocyanin (red). The solid line correspond to the SAC of all the pigments in PROSPECT-D, the dashed lines to the SAC of chlorophylls and carotenoids in PROSPECT-5, and to the SAC of anthocyanins measured by Peters and Noble (2014) using thin layer chromatography.](image-url)
Table 2
RMSE (μg cm⁻²) of the estimation of leaf pigment content using PROSPECT-3 (P-3), PROSPECT-5 (P-5), and PROSPECT-D (P-D) inversion. The bold font for numbers indicates the lowest values.

<table>
<thead>
<tr>
<th>Database</th>
<th>C_{ab} P-3</th>
<th>P-5</th>
<th>P-D</th>
<th>C_{ac} P-3</th>
<th>P-5</th>
<th>P-D</th>
<th>C_{match} P-3</th>
<th>P-5</th>
<th>P-D</th>
</tr>
</thead>
<tbody>
<tr>
<td>CALIBRATION</td>
<td>6.84</td>
<td>3.69</td>
<td>3.43</td>
<td>6.89</td>
<td>1.31</td>
<td>1.74</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ANGERS (VAL)</td>
<td>11.07</td>
<td>6.71</td>
<td>7.07</td>
<td>6.90</td>
<td>3.81</td>
<td>3.22</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MAPLE</td>
<td>15.54</td>
<td>7.85</td>
<td>3.28</td>
<td>17.28</td>
<td>2.23</td>
<td>2.34</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>VIRGINIA (VAL)</td>
<td>14.38</td>
<td>7.74</td>
<td>2.95</td>
<td>17.41</td>
<td>1.19</td>
<td>4.54</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>DOGWOOD-1</td>
<td>14.94</td>
<td>7.90</td>
<td>3.12</td>
<td>18.07</td>
<td>1.21</td>
<td>2.24</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>HAZEL</td>
<td>20.88</td>
<td>9.67</td>
<td>2.36</td>
<td>n.a.</td>
<td>n.a.</td>
<td>2.82</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>DOGWOOD-2</td>
<td>37.22</td>
<td>16.51</td>
<td>6.08</td>
<td>20.92</td>
<td>10.92</td>
<td>14.39</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>VALIDATION</td>
<td>13.33</td>
<td>7.33</td>
<td>5.58</td>
<td>12.67</td>
<td>3.06</td>
<td>3.49</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The calibration followed a two-steps algorithm described in Féret et al. (2008). First, we determined the structure parameter \( N_j \) of each leaf \( j \) in the calibration datasets on the basis of an iterative optimization: \( N_j \) was estimated based on a multivariate iterative optimization, simultaneously with three absorption coefficients using reflectance and transmittance values measured at three wavelengths corresponding to the minimum absorptance \( \lambda_1 \), maximum reflectance \( \lambda_2 \), and maximum transmittance \( \lambda_3 \) of the leaf. These values are generally located on the NIR plateau. The iterative optimization was performed using the merit function:

\[
M_{\text{depth}}(N_j, k(\lambda_1), k(\lambda_2), k(\lambda_3)) = \sum_{i=1}^{3} \left( \frac{R_{\text{meas}}(\lambda_i) - R_{\text{mod}}(N_j, k(\lambda_i))}{r} \right)^2 + \left( \frac{T_{\text{meas}}(\lambda_i) - T_{\text{mod}}(N_j, k(\lambda_i))}{r} \right)^2
\]

with \( R_{\text{meas}}(\lambda_i) \) and \( T_{\text{meas}}(\lambda_i) \) the measured reflectance and transmittance of leaf \( j \) at the wavelength \( \lambda_i \), \( R_{\text{mod}} \) and \( T_{\text{mod}} \) the modeled values, and \( k(\lambda) \) the absorption coefficient of a compact layer at the wavelength \( \lambda \), which is adjusted simultaneously with \( N_j \). In Eq. (3), \( k(\lambda) \) is not decomposed into specific absorption of the different chemical constituents. This step occurs in the NIR where pigments have little if any influence, so \( k(\lambda) \) is primarily affected by water absorption.

The SAC to be calibrated were then computed by inverting PROSPECT on the \( n = 164 \) leaves of the calibration dataset. We minimized the merit function \( J \) at each wavelength:

\[
J(\{K_{\text{spe},i}(\lambda_j)\}_{i=1,n}) = \frac{\sum_{i=1}^{n} \left( R_{\text{meas},i}(\lambda_j) - R_{\text{mod},i}(N_j, k(\lambda_i)) \right)^2}{\sum_{i=1}^{n} \left( T_{\text{meas},i}(\lambda_j) - T_{\text{mod},i}(N_j, k(\lambda_i)) \right)^2}
\]

where

\[
k(\lambda) = \frac{\sum K_{\text{spe},i}(\lambda) \times C_{i,j}}{N_j}
\]

\( k(\lambda) \) is the absorption coefficient of a compact layer at the wavelength \( \lambda \), \( K_{\text{spe},i}(\lambda) \) is the SAC of constituent \( i \), \( C_{i,j} \) is the corresponding content for leaf \( j \), \( N_j \) is the leaf structure parameter of leaf \( j \), and \( n \) corresponds to the number of biochemical constituents for which the SACs are simultaneously calibrated.

3. Validation: datasets and criteria for the comparison of model performances

We performed model inversions on the validation dataset with PROSPECT-D, as well as PROSPECT-3 and -5. The performances of the different versions of the model were compared in terms of pigment

Fig. 6. Estimation of pigment content by inversion of three versions of PROSPECT on six datasets (when relevant). Red dots correspond to calibration samples from ANGERS and VIRGINIA. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
content estimation and leaf spectra fit. The validation was performed using all leaf samples after exclusion of the calibration samples.

PROSPECT was inverted on the validation dataset using an iterative method for optimization. It consists in finding the best combination of leaf chemical and structural parameters that minimizes the merit function:

\[ M_{\text{inv}}(N, \{C_i\}_{i=1:p}) = \sum_{n=1}^{N_{\text{bands}}} (R_{\text{meas},\lambda} - R_{\text{mod},\lambda}(N, \{C_i\}_{i=1:p}))^2 + (T_{\text{meas},\lambda} - T_{\text{mod},\lambda}(N, \{C_i\}_{i=1:p}))^2 \]

where \(n\) the number of available spectral bands, \(N\) the leaf structure parameter, \(C_i\) the content of constituent \(i\), and \(p\) the number of leaf biochemical constituents. In this study, we simultaneously estimated the six input parameters of PROSPECT: pigments \((C_{\text{Cab}}, C_{\text{Cxc}}, C_{\text{Canth}})\), equivalent water thickness \((EWT)\), leaf mass per area \((LMA)\) and leaf structure parameter \((N)\).

In essence, candidate sets of these parameters are iteratively input in forward mode and the resulting modeled reflectance and/or transmittance spectra compared against the measured ones; the parameters are revised until the minimum value of the merit function is found. When the assumptions of the model are not met, for example if a pigment is not taken into account, or if the SACs are incorrect, the inversion will converge towards a suboptimal solution, inducing errors in the estimation of the parameters. This situation occurs when we try to invert PROSPECT-3 on yellowing leaves; \(C_{\text{Cab}}\) is overestimated to compensate for the absorption of \(C_{\text{Cxc}}\).

The root mean square error (RMSE expressed in \(\mu g \text{ cm}^{-2}\)) can be computed to appraise the difference between the measured and estimated pigment content:

\[ \text{RMSE} = \sqrt{\frac{\sum_{j=1}^{n} (X_{\text{meas},j} - X_{\text{mod},j})^2}{n}} \]

where \(X_{\text{meas},j}\) are the measured values and \(X_{\text{mod},j}\) are the values estimated by model inversion for leaf \(j\). As for the quality of the fit, it is appraised by the spectral RMSE which calculates the difference between the measured and simulated reflectance and transmittance spectra on a wavelength-by-wavelength basis.

4. Results

4.1. Selection of a calibration dataset

Fig. 3 shows the pigment distribution corresponding to the calibration and validation samples in ANGERS and VIRGINIA: note that the calibration samples display low to moderate \(C_{\text{Cab}}\) and \(C_{\text{Cxc}}\) values, whereas the validation samples encompass significantly broader pigment contents. The calibration samples with high \(C_{\text{Canth}}\) come from VIRGINIA, for reasons explained earlier.

4.2. Selection of the refractive index

The refractive index spectra displayed in Fig. 2 provide advantages and disadvantages in terms of model accuracy both for the estimation of leaf chemistry and the simulation of leaf optical properties. We performed calibrations of PROSPECT-D as detailed in Section 3, using either the refractive index of PROSPECT-3 and the one derived by Chen and Weng (2012). Then we inverted the two versions of the model on ANGERS, the only dataset covering the SWIR as well as including measurements of \(EWT\) and \(LMA\). Overall the performances obtained for pigment retrieval and simulation of leaf optics were similar in the VIS. For water and dry matter, results were also very similar. Simulated leaf reflectance and transmittance spectra also exhibited very slight differences in the VIS, while they were noticeable in the NIR and SWIR. This is illustrated by Fig. 4 that displays the spectral RMSE calculated between measured and simulated leaf spectra for ANGERS. The reflectances are comparable, with slightly higher RMSE obtained with the refractive index derived from Chen and Weng (2012) between 1500 nm and 1900 nm; there are higher discrepancies in the transmittances. Based on these results, we assigned the refractive index used in PROSPECT-3 to PROSPECT-D.

4.3. Adjustment of the specific absorption coefficients

Fig. 5 displays the SACs of pigment in PROSPECT-5 and PROSPECT-D. The differences between the two models are minor for chlorophylls and carotenoids beyond 450 nm. However, noticeable differences can be observed for carotenoids between 400 nm and 450 nm: compared to PROSPECT-D, the SAC of \(C_{\text{Cxc}}\) sharply increases towards the ultraviolet (UV) domain in PROSPECT-5, possibly due to the presence of flavonoids in the calibration samples. This augmentation is compensated by a slight
4.4.1. Estimation of leaf pigment by PROSPECT inversion

\( \text{C}_{\text{ab}}, \text{C}_{\text{xc}}, \text{and C}_{\text{canth}} \) have been estimated by inversion of PROSPECT-D on a dataset hereafter called VALIDATION. It gathered all experimental datasets (Table 1) except DOGWOOD-2 which did not contain transmittance spectra. ANGERS was also excluded for anthocyanins since \( \text{C}_{\text{canth}} \) has been indirectly estimated using a spectral index.

Table 2 compares the performances of PROSPECT-3, -5 and -D for pigment estimation in terms of RMSE. One can note a markedly improvement of \( \text{C}_{\text{xc}} \) estimation by PROSPECT-D for all datasets. In ANGERS, which mainly contain green leaves, PROSPECT-5 and PROSPECT-D perform similarly at estimating \( \text{C}_{\text{ab}} \) with a slight increase of RMSE obtained with PROSPECT-D. It can be explained by the fact that these samples correspond to calibration samples in PROSPECT-5. PROSPECT-D surpasses the previous versions of the model for all datasets other than ANGERS. Importantly, the new model is able to accurately estimate \( \text{C}_{\text{xc}} \) even in anthocyanic leaves, which has been problematic for other techniques.

Fig. 6 illustrates the differences observed in Tables 2. PROSPECT-3 underestimated \( \text{C}_{\text{ab}} \) for all datasets, even with ANGERS which mainly contained green leaves; this overestimation was reduced when using PROSPECT-5 or PROSPECT-D. The substantial improvement in \( \text{C}_{\text{xc}} \) estimation when using PROSPECT-D is a significant result of this article: overall, the RMSE was divided by four compared to the results obtained with PROSPECT-5. The inversion of PROSPECT-5 on anthocyanin-rich leaves sometimes converged towards the upper bound on \( \text{C}_{\text{xc}} \) (30 \( \mu g \) cm\(^{-2} \)). It is likely that this overestimation of carotenoid content results from the strong absorption of light by anthocyanins in the same wavelength range as carotenoids, and this absorption is not properly modeled by PROSPECT-5. In ANGERS, the systematic underestimation of \( \text{C}_{\text{xc}} \) by PROSPECT-5 in leaves containing high amounts of photosynthetic pigments was greatly reduced by PROSPECT-D. The overestimation of \( \text{C}_{\text{xc}} \) in anthocyanin-rich leaves was also corrected. The lower performances of PROSPECT-D on DOGWOOD-2 are probably explained by the absence of transmittance spectra. As explained in Section 4.1, the samples selected for the calibration dataset in ANGERS were marked out by low to medium pigment content, therefore they were not representative of the full range of variation found in this dataset: nevertheless, this did not prevent us from estimating high pigment content with accuracy. This is explained by slight changes in the optical properties of leaves with high-pigment content when carotenoids increase, due to saturation effects. It also suggests that the physical description used in PROSPECT is correct, as its ability to estimate pigment content goes beyond the range used for calibration. Samples showing underestimated \( \text{C}_{\text{xc}} \) in ANGERS were discarded from the calibration dataset due to unusual optical properties (surface effects) or very high mARI.

4.4.2. Spectrum reconstruction

We compared the spectral RMSE between measured spectra and spectra reconstructed by the last three versions of PROSPECT after model inversion on the VALIDATION dataset (Fig. 7). Values obtained with PROSPECT-3 ranged between 2% and 6% over the VIS. This model uses a unique SAC to account for total pigment absorption; therefore it solely applies to healthy green leaves. The dissociation of chlorophylls from carotenoids in PROSPECT-5 explains the strong decrease in RMSE between 400 nm and 500 nm where carotenoids absorb light. However, the discrepancies are still strong between 500 nm and 600 nm where anthocyanins absorb light, and between 650 nm and 750 nm, a spectral domain that corresponds to the second absorption peak of chlorophylls. Finally, PROSPECT-D surpassed the previous versions with RMSE ranging between 1% and 2% over the entire VIS.

Fig. 10. Spectral RMSE between measured and estimated leaf reflectance and transmittance obtained for the VALIDATION dataset after model inversion using PROSPECT-D calibrated with (grey lines) and without (red lines) uncertainty added to \( \text{C}_{\text{canth}} \). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
4.5. Sensitivity to the uncertainty associated with \( C_{\text{anth}} \) in ANGERS

4.5.1. Specific absorption coefficients

The addition of noise to \( C_{\text{anth}} \) in ANGERS influences the calibration of the SACs of PROSPECT, as expected, but the variability is limited to the 400–500 nm wavelength range, especially for anthocyanins. The main difference for this pigment is observed between 500 nm to 600 nm (Fig. 8).

4.5.2. Estimation of pigment content

We estimated pigment content by inverting PROSPECT with the set of SACs derived from noisy \( C_{\text{anth}} \). Fig. 9 summarizes the distributions of RMSE from measured and estimated pigment contents for the validation datasets taken separately and for the VALIDATION dataset that group them together. The uncertainty on \( C_{\text{anth}} \) has no influence on the estimation of \( C_{\text{cab}} \) as the RMSE is close to that obtained when no noise was added to \( C_{\text{anth}} \). The influence is higher on the estimation of carotenoids. The version of the model with no noise added to \( C_{\text{anth}} \) outperformed the versions including noise, particularly for MAPLE. This version also outperformed all noisy versions when focusing on VALIDATION. Finally, the estimation of \( C_{\text{anth}} \) also performed better when no noise was added to the ANGERS calibration samples, except for MAPLE, which performs a little less now. However as for \( C_{\text{cab}} \), the results obtained with VALIDATION showed better estimation of \( C_{\text{anth}} \) when no noise was added. These results validate the calibration of PROSPECT-D with \( C_{\text{anth}} \) determined using a spectral index. Moreover, the slight decrease in performances for the estimation of \( C_{\text{ans}} \) and \( C_{\text{x}} \) when adding noise to \( C_{\text{anth}} \) suggests that the estimated values obtained for \( C_{\text{anth}} \) in ANGERS may show lower uncertainty than expected based on the experimental data available.

4.5.3. Simulation of leaf optical properties

The accuracy of reflectance and transmittance reconstruction is displayed in Fig. 10. The spectra simulated by PROSPECT-D show very minor differences whatever noise was added to \( C_{\text{anth}} \) or not. These results confirm that despite missing values and indirect estimation of \( C_{\text{anth}} \) for ANGERS, PROSPECT-D provides stable results in terms of calibrated SACs as well as model performance both in direct and inverse modes.

5. Discussion

5.1. Specific absorption coefficients

As stated earlier, the SAC of anthocyanins obtained after the calibration phase (Fig. 5) displayed a broad absorption peak centered on 550 nm. The overall profile agrees well with the spectra obtained in previous studies (Gitelson et al., 2001; Peters and Noble, 2014). We compared this SAC with absorption spectra of pure cyanidin-3-glucoside (C3G), measured in the lab for different pH (Fossen et al., 1998). C3G is also the most common anthocyanin in leaves (Harborne and Williams, 1998). The SACs derived from a model generally do not match data published in the literature for in vitro dissolved pigments. Several causes may explain such a discrepancy. First, radiative transfer model are imperfect: for instance, a two-layer model taking into account the asymmetry of leaf anatomy and chemical content in Dicots may improve the determination of the SACs. Moreover, the calibration of these models is based on experimental data which may be not optimal in terms of sampling, despite our efforts to provide the best experimental datasets. Second, molecules in vivo are linked to their environment, which may induce shifts in their SACs: this is the case for chlorophylls with proteins, or anthocyanins with the pH or temperature (Figueiredo et al., 1999; Yabuya et al., 1997; Boulton, 2001). Thirdly, while the model assumes stable compositions and absorption spectra for chlorophylls, carotenoids and anthocyanins, in reality these are families of pigments containing between two and hundreds of molecules, with as many variations in their particular absorption spectra. Subtle changes in anthocyanin composition, chlorophyll \( a:b \) ratio, or induced by the xanthophyll cycle may result in variations in leaf reflectance and transmittance that are detectable but not interpretable by PROSPECT. Finally, as explained earlier, internal multiple scattering (detour effect) and distributional errors (sieve effect) may also explain part of

Fig. 11. Comparison of the SAC corresponding to anthocyanins derived from PROSPECT-D calibration (cm\(^2\) μg\(^{-1}\)) and the absorption of pure Cyanidin 3-glucoside at pH 1 and 8.1 (unitless) (after Fossen et al., 1998).

Fig. 12. Measured (black dotted line) versus simulated (blue line for PROSPECT-5 and red line for PROSPECT-D) reflectance (lower spectra) and transmittance (upper spectra). (a–b) Acer pseudoplatanus L., (c) Acer platanoides L., (d) Corylus avellana L., (e–f) Parthenocissus quinquefolia (L.) Planch., (g) Corylus maxima ‘Purpurea’, and (h) Eucalyptus gunnii. Samples (b–e–f) show non-senescent anthocyanic leaves, while samples (a–c–d–g) show anthocyanic senescent leaves. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
the discrepancies observed between in vivo and in vitro SACs. Fig. 11 shows the profile of the SAC of anthocyanins: it is intermediate between the absorption coefficient measured for C3G at pH 1 and pH 8.1 in the main absorption domain of this constituent. The increasing absorption closer to the UV-A may be explained by the presence of flavonols in some leaves: these molecules, which are biosynthetically associated with anthocyanins in plant secondary metabolism, are also optically active in this domain. Therefore, it is likely that flavonols contribute to the anthocyanin SAC spectrum (Solovchenko et al., 2001). The improvement of \( C_{\text{av}} \) estimation accuracy upon incorporation of anthocyanins into PROSPECT-D may stem from the inherent correlation between anthocyanin and flavonoid content.

The SAC of carotenoids above 450 nm is very similar in PROSPECT-5 and PROSPECT-D. However the estimation of \( C_{\text{av}} \) is substantially improved in the latter, which highlights the high sensitivity of PROSPECT to very small changes of the SAC, as well as the importance of incorporating anthocyanins into the model even for leaves with low content. This improvement in the estimation of \( C_{\text{av}} \) was not explained by the differences observed between 400 nm and 450 nm: when using all the ANGERS dataset for calibration, the SAC calibrated for \( C_{\text{av}} \) showed very similar profile as in PROSPECT-5, but the improvement in the estimation of \( C_{\text{av}} \) was still observed.

5.2. Illustration of the improved simulation of leaf optical properties

To illustrate the ability of PROSPECT-D to simulate leaf optical properties we selected some samples including senescent and reddish leaves (Fig. 12). In some cases, the fit is poor: the reflectance spectrum of Eucalyptus gunnii is very high compared to that of other leaves, probably due to the presence of wax at the leaf surface, a layer that is not accounted for in PROSPECT (Fig. 12h). Barry and Newnham (2012) already pointed out an incorrect assessment of carotenoid content in Eucalyptus globulus and Eucalyptus nitens leaves. The development of PROSPECT-D partly answers these limitations, but further efforts will be needed to include specular reflection (Bouquet et al., 2005; Comar et al., 2014; Jay et al., 2016).

6. Conclusion

We introduced a new, physically-based model called PROSPECT-D which, for the first time, includes the three main families of leaf pigments as independent constituents: chlorophylls, carotenoids, and anthocyanins. PROSPECT-D outperformed the previous versions of the model, both for the estimation of leaf chemical constituents and the simulation of leaf optical properties, on datasets encompassing a broad range of growth conditions and stages. Inversion of PROSPECT-D showed improved estimation of pigment content, especially carotenoid content. These results demonstrate the ability of this new model to simulate optical properties during the lifespan of the leaf and for a new range of conditions, including juvenile and senescent stages, as well as environmental stresses.

We studied the influence of the uncertainty corresponding to the values of \( C_{\text{av}} \) from ANGERS used for the calibration of PROSPECT-D. Our results showed that this uncertainty has little to no impact on the calibration, and on the performances of the model in terms of pigment prediction accuracy, as well as in modeling of leaf optics.

The availability of this model has strong implications for vegetation modeling both at leaf and canopy scales. At the leaf scale, PROSPECT-D will allow to perform sensitivity analyses focused on anthocyanins, and to design new vegetation indices dedicated to specific pigments and less sensitive to other ones. The linkage of PROSPECT-D with canopy reflectance models such as SAIL (e.g., Jacquesmoud et al., 2009) or DART (Hernández-Clemente et al., 2012; Gastelu-Etchegorry et al., 2015) will allow simulations of vegetation types that could not be reproduced before. Applications for stress and senescence detection will directly take advantage of such improvements. Finally PROSPECT-D is a powerful tool for determining the potential of operational multispectral satellites (Sentinel-2, Landsat-8, WorldView-3) and future hyperspectral missions (EnMAP, Hypsir, HYPXIM) for fine detection of leaf pigments.

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